

Estimating ancestry from a population kinship matrix under arbitrary ancestral subpopulation structure

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Disclosure Slide

Financial Disclosure for:

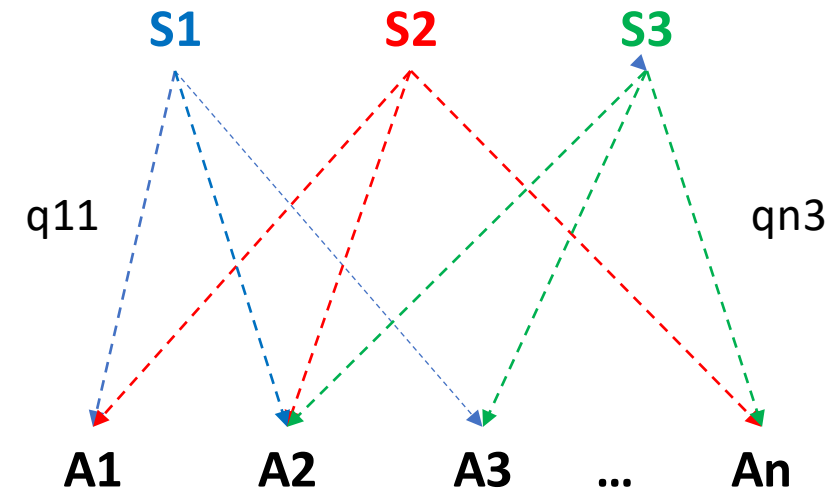
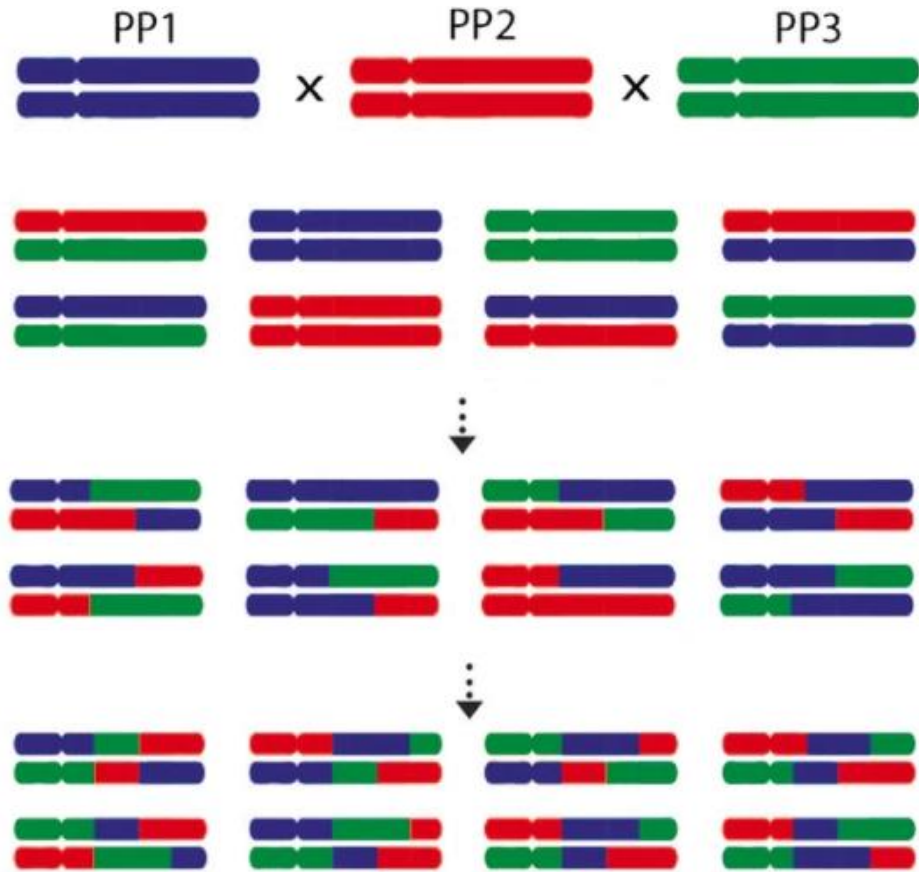
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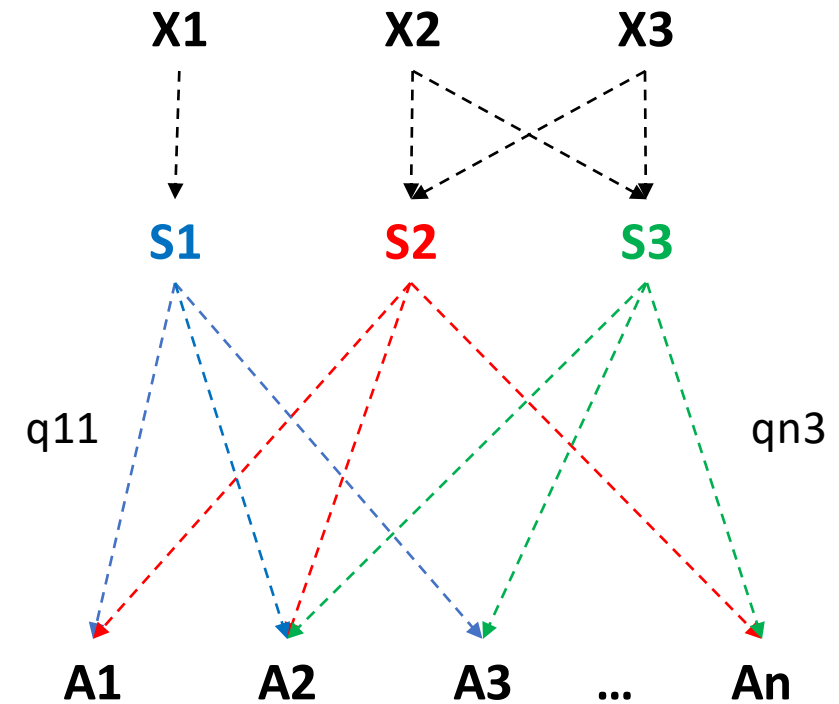
I have nothing to disclose

Motivation



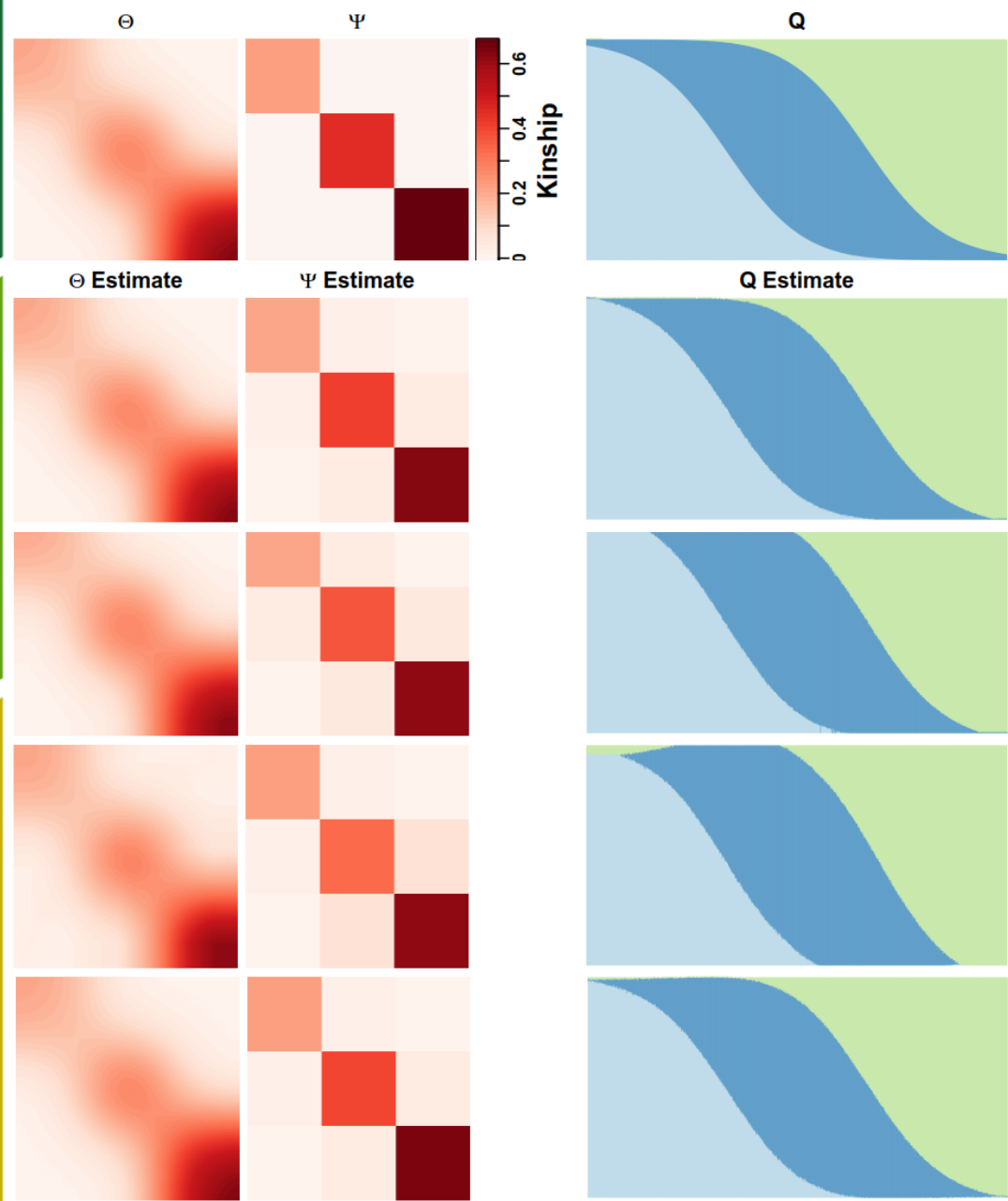
Model and Data Generation

- $P \in \mathbb{R}^{m \times k}$, $p_{ij} \in [0,1]$
- $Q \in \mathbb{R}^{n \times k}$, $q_{ij} \geq 0$, $\sum_j q_{ij} = 1$
- $\pi = PQ^T$
- The coancestry matrix of P should equal the coancestry of the ancestral/intermediate subpopulations, Ψ .



Performance of existing approaches

Independent ancestral populations



Admixture:
Model-based ancestry estimation

fastStructure :
Variational Bayesian framework

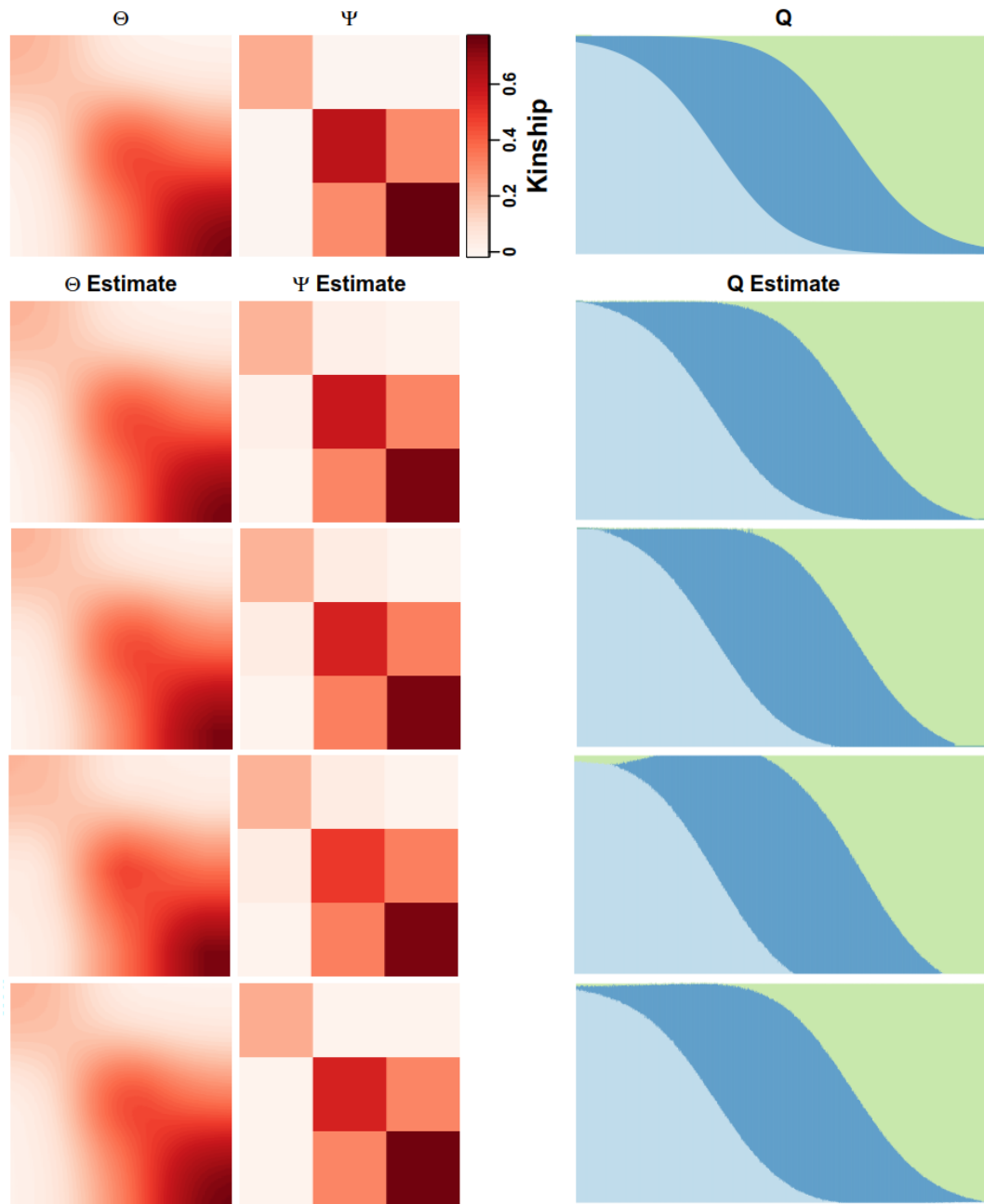
sNMF:
NMF and least-squares optimization

ALStructure:
PCA based method

- 1000 individuals
- 100,000 loci
- 3 populations
- $F_{ST} = 0.3$

Performance of existing approaches

Correlated ancestral populations



Admixture:
Model-based ancestry estimation

fastStructure :
Variational Bayesian framework

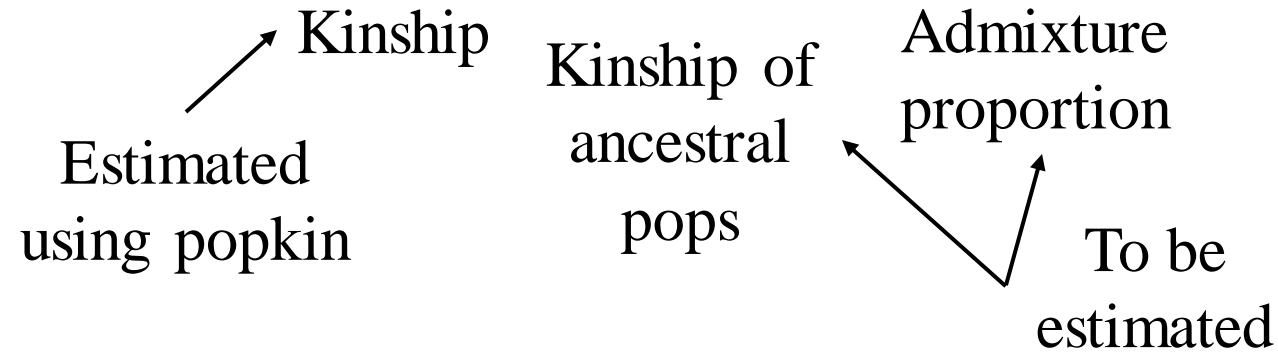
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Optimization

$$\Theta = Q\Psi Q^T$$

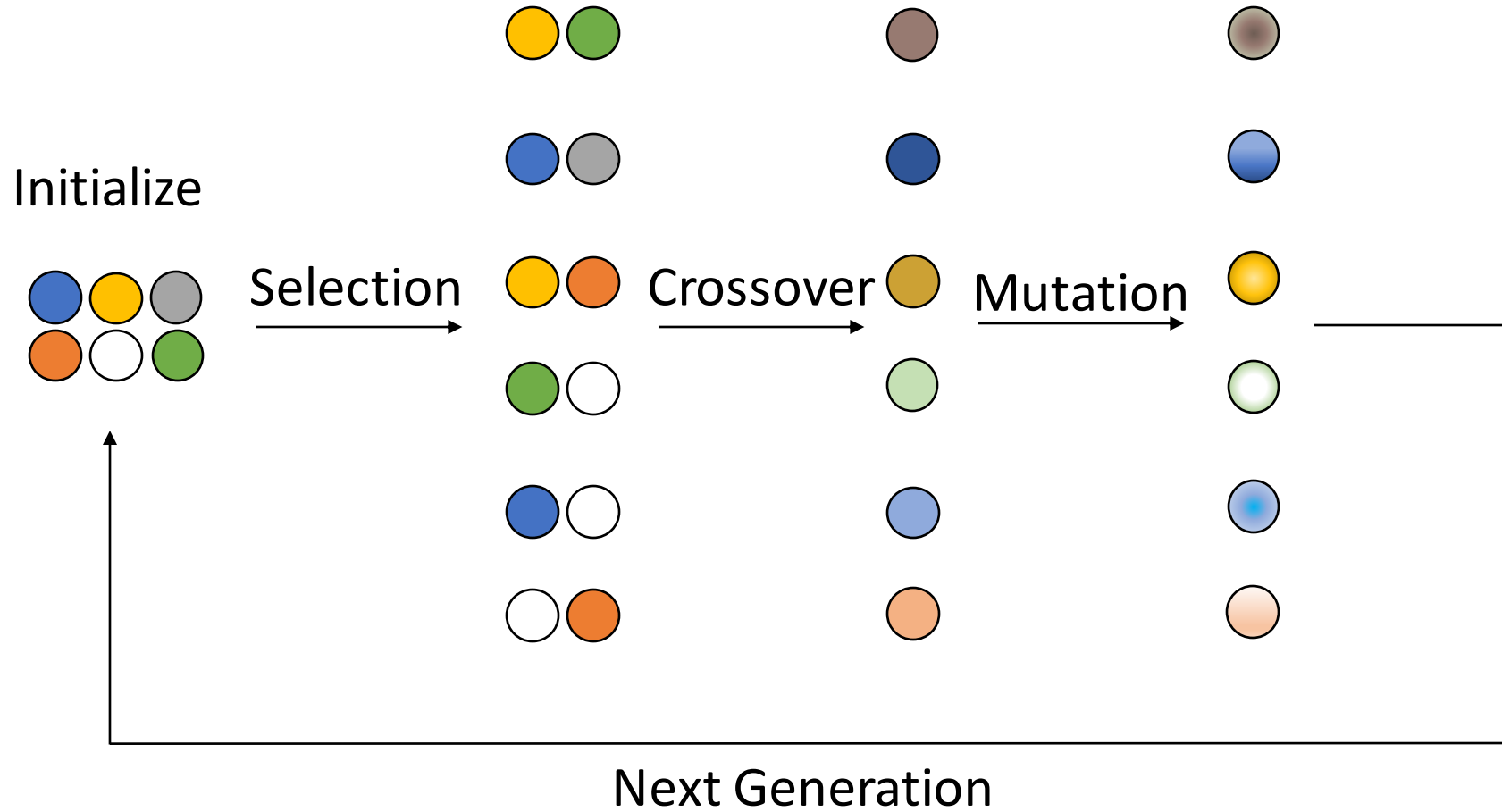


$$F = \|Q\Psi Q^T - \Theta\|^2$$

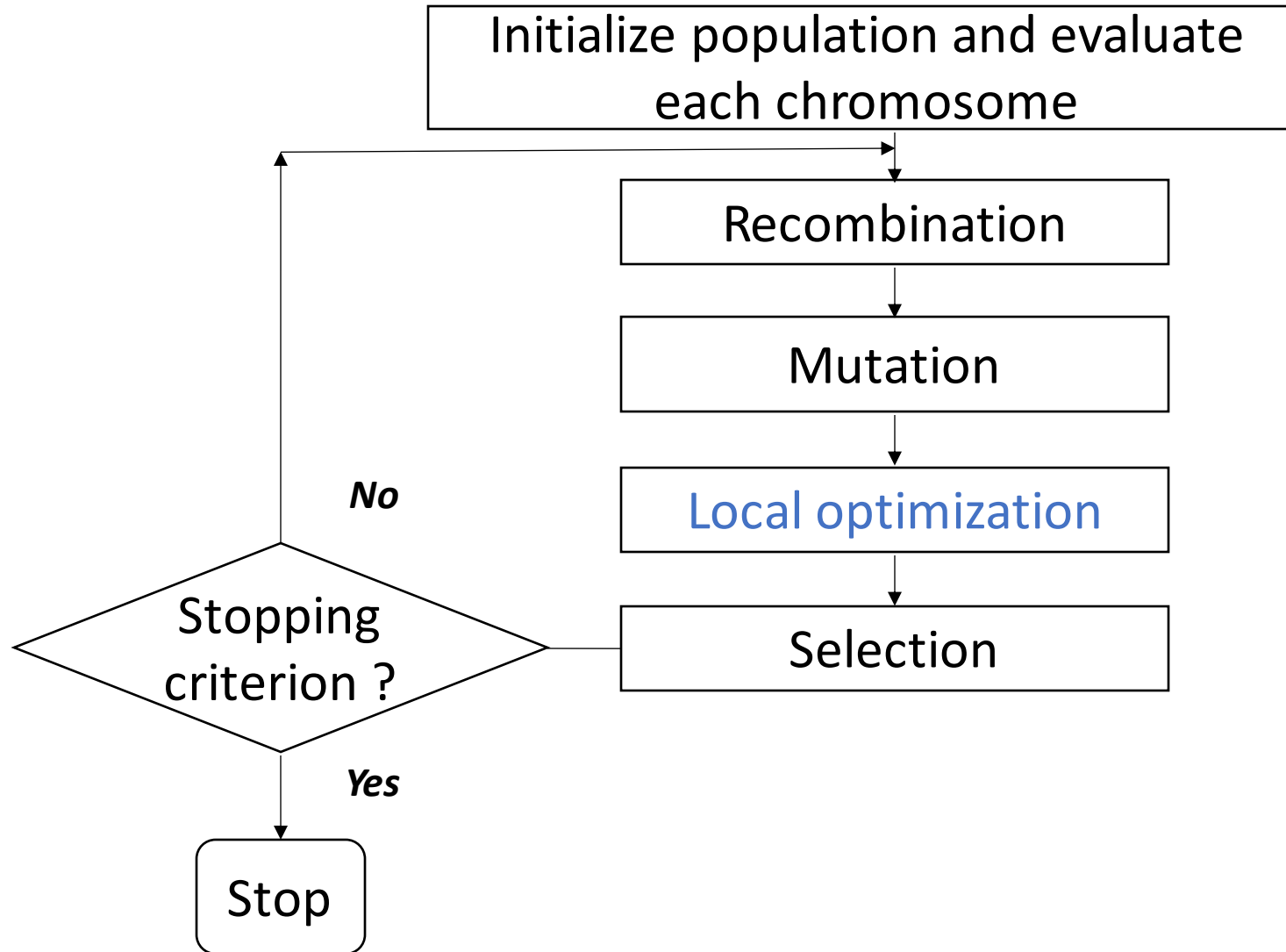
- Multiple minima problem,
- Factorization is not unique.

$$Q' = QR$$
$$\Psi' = R^{-1}\Psi(R^{-1})^T$$

Genetic Algorithm

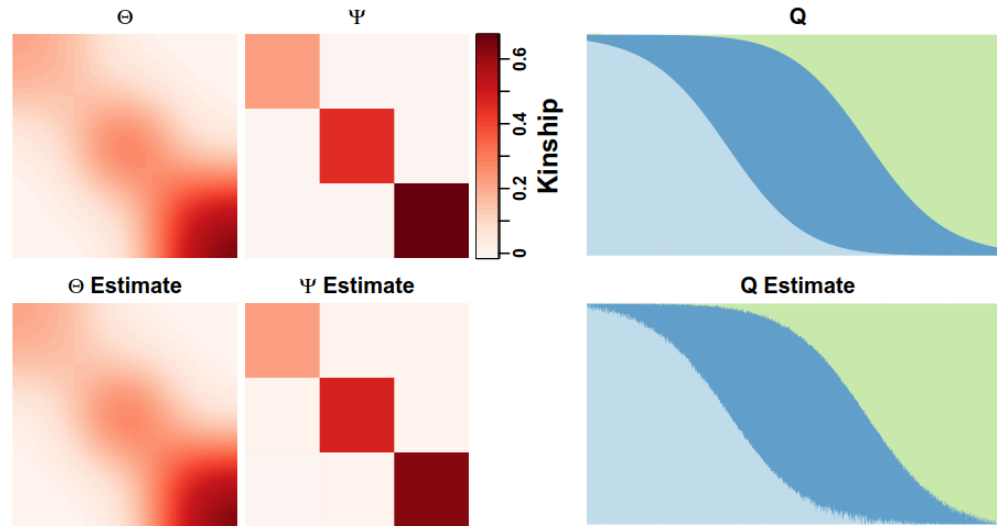


Memetic Algorithm

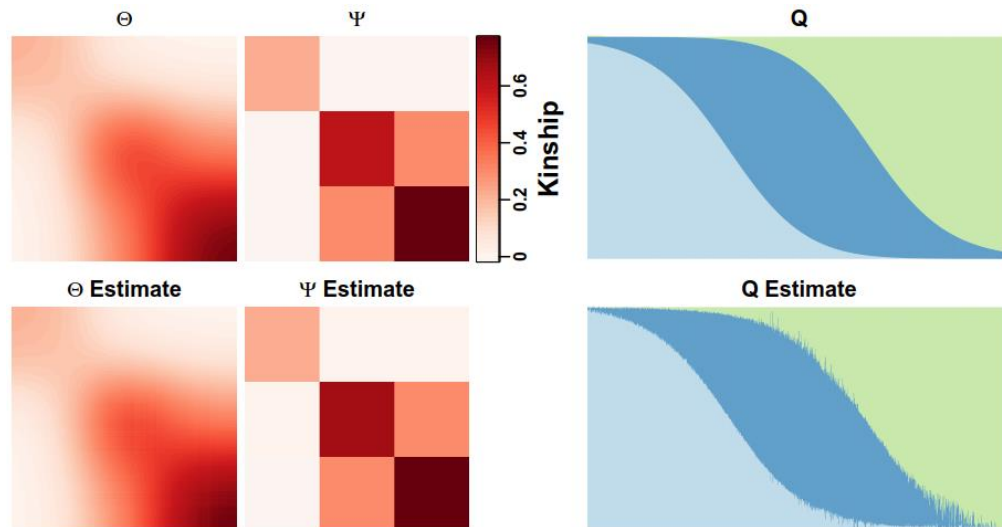


Memetic Algorithm

Independent
ancestral
populations

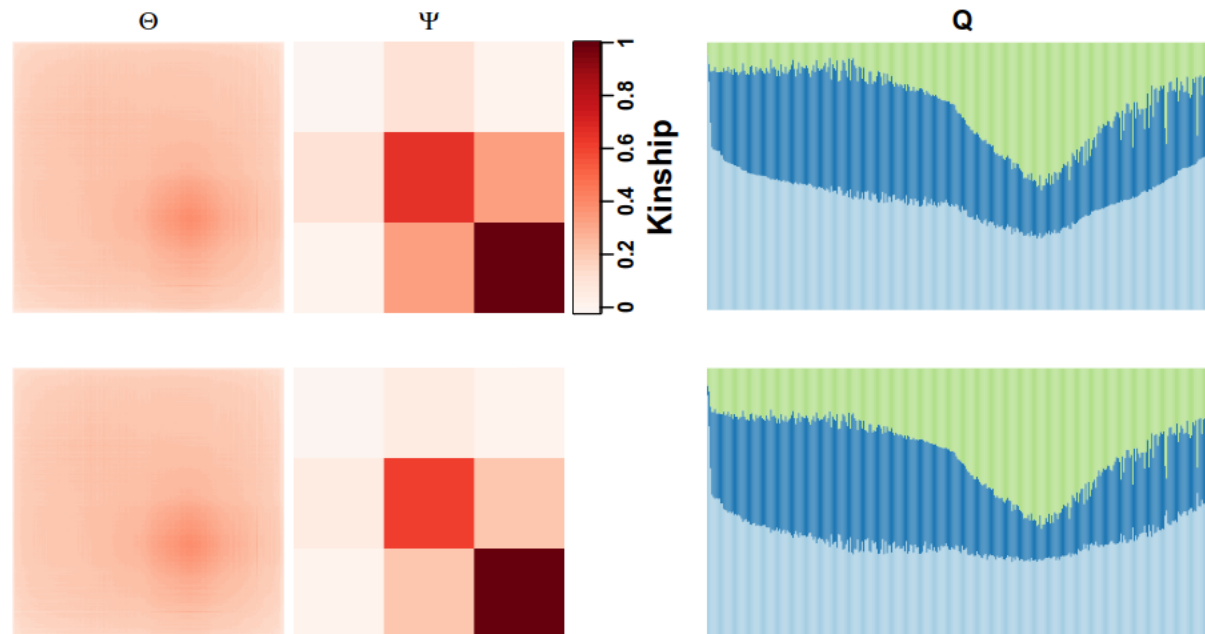


Correlated
ancestral
populations



- 1000 individuals,
- 100, 000 loci, and
- 3 subpopulations

Hispanic individuals in the 1000 Genomes Project



Admixture

6.7 million high-frequency SNPs

Memetic Algorithm

347 individuals

Conclusion and Next steps



- First likelihood free approach to jointly estimate admixture and kinship between ancestral subpopulations without bias.
- Estimated from a kinship matrix only.
- Not dependent on the number of loci, therefore run time is only dependent on the number of individuals and populations.

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